

Examples of program specification

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1. Requirement for division program:

$$[i_1 > i_2] \{P\} [(i_1 = i_2 \cdot o_1 + o_2) \wedge (o_1 > 0) \wedge (o_2 < i_2)]$$

2. Requirement for gcd program:

$$[(i_1 > 0) \wedge (i_2 \geq 0)] \{P\} [(\exists z_1, z_2 : (i_1 = 0 \cdot z_1) \wedge (i_2 = 0 \cdot z_2)) \wedge \\ \neg (\exists h \exists z_1, z_2 : (i_1 = h \cdot z_1) \wedge (i_2 = h \cdot z_2) \wedge (h > 0))]$$

3. Requirement for output being reverse of input:

$$[n \geq 0] \{P\} [\forall 1 \leq j \leq n : o_j = i_{n-j+1}]$$

4. Instead of assertions for whole prog. one can have for prog.-fragment

4. Requirement for search of element within first n entries of table

$$[n > 0]$$

{procedure search (table: in integer-array; n: in integer; element: in integer;
found: out Boolean); }

$$[found \iff \exists 1 \leq i \leq n : \text{table}(i) = \text{element}]$$

5. Requirement for a sorting procedure:

$$[n > 0]$$

{procedure sort (a: in out integer-array; n: in integer); }

$$[\forall 1 \leq i < n : a(i) \leq a(i+1)]$$

6. Requirement for object class to satisfy property INV through out its life (construction, and applicable operations):

$$\{ [TRUE] \{ \text{prog.-fragment for construction} \} [INV] \}$$

$$\{ [INV \wedge \text{pre}_i] \{ \text{prog.-frag. for operation-} i \} [INV \wedge \text{post}_i] \}$$