## Mohr's Circle

Mohr's Circle is a graphic interpretation of the stress transformation equations:

$$\boldsymbol{s}_{n} - \frac{\boldsymbol{s}_{x} + \boldsymbol{s}_{y}}{2} = \frac{\boldsymbol{s}_{x} - \boldsymbol{s}_{y}}{2} \cos(2\boldsymbol{q}) + \boldsymbol{t}_{xy} \sin(2\boldsymbol{q})$$
$$\boldsymbol{t}_{nt} = -\frac{\boldsymbol{s}_{x} - \boldsymbol{s}_{y}}{2} \sin(2\boldsymbol{q}) + \boldsymbol{t}_{xy} \cos(2\boldsymbol{q})$$

It can be shown that a circle can be formed in terms of  $\sigma_n$  and  $\tau_{nt}$ 

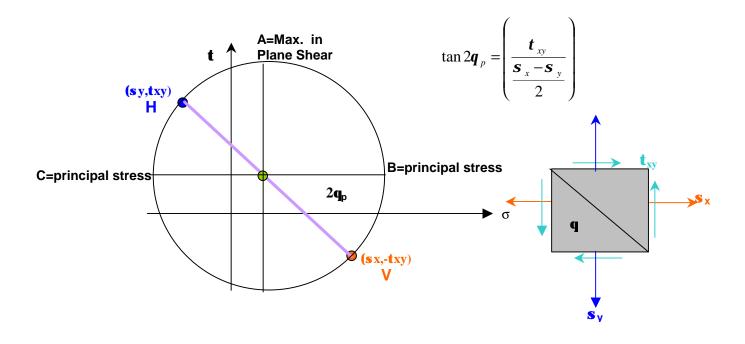
The radius of the circle is:

$$r = \sqrt{\left(\frac{\boldsymbol{q}_x - \boldsymbol{q}_y}{2}\right)^2 + \boldsymbol{t}^2_{xy}}$$

Normal stresses are plotted on a horizontal axis; positive stress plotted to the right, and negative stresses to the left. Shearing stresses are plotted on the vertical axis.

Steps in creating a Mohr's Circle

- 1. Choose a set of x-y axis
- 2. Identify stresses  $\sigma x$ ,  $\sigma y$  and  $\tau x y$  with proper signs.
- 3. Plot  $(\sigma x, -\tau xy)$  and label this point V
- Plot (σy, τxy) and label this point H
  Draw a line connecting V and H; this establishes the center of the circle, C
- 6. Draw the circle
- 7. Label pertinent points, principal stresses, orientation in plane



Example:

Plot the Mohr's circle that represents the stress element shown

